



**NAMIBIA UNIVERSITY  
OF SCIENCE AND TECHNOLOGY**

**FACULTY OF HEALTH AND APPLIED SCIENCES**

**DEPARTMENT OF MATHEMATICS AND STATISTICS**

<b>QUALIFICATION:</b> Bachelor of science Honours and Applied and Statistics	
<b>QUALIFICATION CODE:</b> 08BSSH	<b>LEVEL:</b> 8
<b>COURSE CODE:</b> SAT802S	<b>COURSE NAME:</b> SAMPLING THEORY
<b>SESSION:</b> JANUARY 2019	<b>PAPER:</b> THEORY
<b>DURATION:</b> 3 HOURS	<b>MARKS:</b> 100

<b>SECOND OPPORTUNITY EXAMINATION QUESTION PAPER</b>	
<b>EXAMINER</b>	Dr CR. KIKAWA
<b>MODERATOR:</b>	PROF SATHIYA APPUNNI

<b>INSTRUCTIONS</b>
<ol style="list-style-type: none"><li>1. Answer ALL the questions in the booklet provided.</li><li>2. Show clearly all the steps used in the calculations.</li><li>3. All written work must be done in blue or black ink and sketches must be done in pencil.</li></ol>

**PERMISSIBLE MATERIALS**

1. Non-programmable calculator without a cover.

**THIS QUESTION PAPER CONSISTS OF 5 PAGES** (Including this front page)

NAMIBIA UNIVERSITY OF SCIENCE AND TECHNOLOGY  
DEPARTMENT OF MATHEMATICS AND STATISTICS  
SAMPLING THEORY: SAT802S

EXAMINATION SECOND OPPORTUNITY, JANUARY 2019  
Time - 3 Hrs. Attempt all Questions. Maximum marks - 100

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1. Question (20 marks)
- (a) Discuss the following concepts as used in sampling theory, give relevant examples where applicable:
- i. Sample survey and population census (2 marks)
  - ii. Pre-test/Pilot survey (2 marks)
  - iii. Elementary units or elements (2 marks)
- (b) Write short notes on the concepts; Probability and Non-probability Sampling. (4 marks)
- (c) Discuss why we use the sampling with replacement in sampling theory? (5 marks)
- (d) Write short notes on the usage of auxiliary information with a clear illustration. (5 marks)

2. Question

(20 marks)

The investigator samples 10 one-acre plots by simple random sampling (SRS) and counts the number of trees (y) on each plot. The investigator also has aerial photographs of the plantation from which she can estimate the number of trees (x) on each plot of the entire plantation. Hence, she knows  $\mu_x = 19.7$  and since the two counts are approximately proportional through the origin, she uses a ratio estimate to estimate  $\mu_y$ .

Table 1: To estimate the average number of trees per acre on a 1000- acre plantation

Plot	Actual no. per acre Y	Aerial estimate X	$y_i - rx_i$
1	25	23	0.5625
2	15	14	0.1250
3	22	20	0.7500
4	24	25	-2.5625
5	13	12	0.2500
6	18	18	-1.1250
7	35	30	3.1250
8	30	27	1.3125
9	10	8	1.5000
10	29	31	-3.9375
mean	22.10	20.80	-

(a) Examine figures 1 and 2 and discuss the suitability of using ratio estimates.

(5 marks)

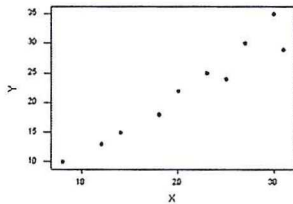


Figure 1: Scatter plot

The regression equation is  
 $Y = 1.24 + 1.00 X$

Predictor	Coef	SE Coef	T	P
Constant	1.239	2.007	0.62	0.554
X	1.00293	0.09094	11.03	0.000

Figure 2: Regression output

(b) Construct the approximate 95% confidence interval for  $\mu_y$

(15 marks)

3. Question (20 marks)
- (a) Discuss the concept a *simple random sample* in relation to  $n$  the sample size and  $N$  the population size clearly stating the selection probability of each sample. (5 marks)
  
  - (b) Assume you have a sample population of  $N$  elements and you wish to take a sample of  $n$  of these elements. Required to state a well known formula from the theory of permutations and combinations which is used to select, the number  $T$  of possible samples of  $n$  elements from a population of  $N$  elements. (4 marks)
  
  - (c) Given that a population contains 25 elements and one wishes to take a sample of 5 elements. Use the relation stated in (b) to compute the possible samples of 5 elements from the population given. (2 marks)
  
  - (d) Explain, stepwise how to take a Simple Random Sample. (4 marks)
  
  - (e) As a researcher you require to use ratio estimates as an estimation method for your analysis, examine Figures 1 and 2 in question (2) and discuss the suitability of your method. (5 marks)

4. Question (20 marks)

(a) Discuss any three practical cases in which multistage sampling designs are used. (6 marks)

(b) Two-stage sampling includes both one-stage cluster sampling and stratified random sampling as special cases.

1. When does two-stage sampling reduce to cluster sampling?  $\hat{\tau}_{st}$  (4 marks)

2. When does two-stage sampling reduce to stratified random sampling?  $\bar{y}_{str}$  (4 marks)

(c) There are 36 departments in a small liberal arts college. One wants to estimate the average amount of money the students spent on textbooks last semester. Since the size of each department varies very much, a two-stage cluster sampling using probability proportional to size for the primary unit is carried out. The results are listed in the table below. Estimate the population mean using probability proportional to size estimator (Hansen-Hurwitz) and estimate the variance of that estimator. (6 marks)

Department	$M_i$	$m_i$	Textbook expenses in S for last semester
1	10	4	326, 400, 423, 443
2	20	8	278, 312, 450, 350, 227, 438, 512, 403
3	30	12	512, 256, 332, 402, 512, 309, 411, 610, 422, 630, 550, 470
4	15	6	426, 312, 512, 440, 342, 533

Figure 3: Table of values



5. Question

(20 marks)

(a) Discuss the concept, *double sampling* clearly stating its major advantages. (6 marks)

(b) A forest resource manager is interested in estimating the total number of dead trees in a 400 acre area of heavy infestation. The manager subdivides the area into 200 plots of equal sizes and uses photo counts to find the number of dead trees in 18 randomly sampled plots. She then randomly samples 8 plots out of these 18 plots and conducts a ground count on these 8 plots.

Note: Study the tables and output given for the estimation of the total number of dead trees in the 400 acre area. So as to answer the questions that follow.

Let  $x$  denote the number of dead trees in the plot by photo count and  $y$  the number of dead trees by ground count. The data are given as:

Plot	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
$x'$	5	7	10	6	7	9	3	6	8	11	5	9	12	13	3	20	15	4

Out of these 18 plots, 8 are randomly selected and a ground count is conducted.

Plot	2	3	5	6	12	15	16	17
$x$	7	10	7	9	9	3	20	15
$y$	9	13	10	11	10	4	25	17
$y-rx$	0.3375	0.6250	1.3375	-0.1375	-1.1375	0.2875	0.2500	-1.5625



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Variable      N      Mean      StDev
x'            18      8.50      4.46
x              8     10.00      5.28
y              8     12.37      6.28

Sum of x' = 153.00, Sum of x = 80.00,
Sum of y = 99.00.

Sum of squares (uncorrected) of y-rx = 6.1928
    
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Figure 4: Tables of values and output

- i. Compute the ratio estimate for the population total. (8 marks)
- ii. compute the estimated variance of the ratio estimator: use the following quantities where applicable

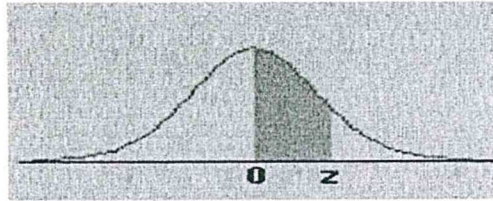
$$s^2 = (st.dev \cdot y)^2 = 6.28^2$$

$$\sum_{i=1}^8 (y_i - r \cdot x_i)^2 = 6.1928$$

(6 marks)

END

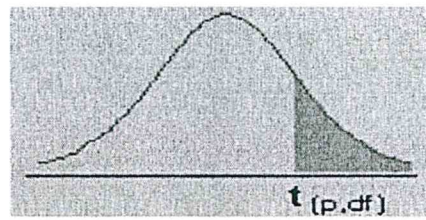
## The Standard Normal Distribution



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990



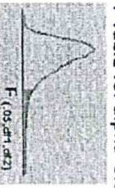
## The t-distribution



df/p	0.40	0.25	0.10	0.05	0.025	0.01	0.005	0.0005
1	0.324920	1.000000	3.077684	6.313752	12.70620	31.82052	63.65674	636.6192
2	0.288675	0.816497	1.885618	2.919986	4.30265	6.96456	9.92484	31.5991
3	0.276671	0.764892	1.637744	2.353363	3.18245	4.54070	5.84091	12.9240
4	0.270722	0.740697	1.533206	2.131847	2.77645	3.74695	4.60409	8.6103
5	0.267181	0.726687	1.475884	2.015048	2.57058	3.36493	4.03214	6.8688
6	0.264835	0.717558	1.439756	1.943180	2.44691	3.14267	3.70743	5.9588
7	0.263167	0.711142	1.414924	1.894579	2.36462	2.99795	3.49948	5.4079
8	0.261921	0.706387	1.396815	1.859548	2.30600	2.89646	3.35539	5.0413
9	0.260955	0.702722	1.383029	1.833113	2.26216	2.82144	3.24984	4.7809
10	0.260185	0.699812	1.372184	1.812461	2.22814	2.76377	3.16927	4.5869
11	0.259556	0.697445	1.363430	1.795885	2.20099	2.71808	3.10581	4.4370
12	0.259033	0.695483	1.356217	1.782288	2.17881	2.68100	3.05454	4.3178
13	0.258591	0.693829	1.350171	1.770933	2.16037	2.65031	3.01228	4.2208
14	0.258213	0.692417	1.345030	1.761310	2.14479	2.62449	2.97684	4.1405
15	0.257885	0.691197	1.340606	1.753050	2.13145	2.60248	2.94671	4.0728
16	0.257599	0.690132	1.336757	1.745884	2.11991	2.58349	2.92078	4.0150
17	0.257347	0.689195	1.333379	1.739607	2.10982	2.56693	2.89823	3.9651
18	0.257123	0.688364	1.330391	1.734064	2.10092	2.55238	2.87844	3.9216
19	0.256923	0.687621	1.327728	1.729133	2.09302	2.53948	2.86093	3.8834
20	0.256743	0.686954	1.325341	1.724718	2.08596	2.52798	2.84534	3.8495
21	0.256580	0.686352	1.323188	1.720743	2.07961	2.51765	2.83136	3.8193
22	0.256432	0.685805	1.321237	1.717144	2.07387	2.50832	2.81876	3.7921
23	0.256297	0.685306	1.319460	1.713872	2.06866	2.49987	2.80734	3.7676
24	0.256173	0.684850	1.317836	1.710882	2.06390	2.49216	2.79694	3.7454
25	0.256060	0.684430	1.316345	1.708141	2.05954	2.48511	2.78744	3.7251
26	0.255955	0.684043	1.314972	1.705618	2.05553	2.47863	2.77871	3.7066
27	0.255858	0.683685	1.313703	1.703288	2.05183	2.47266	2.77068	3.6896
28	0.255768	0.683353	1.312527	1.701131	2.04841	2.46714	2.76326	3.6739
29	0.255684	0.683044	1.311434	1.699127	2.04523	2.46202	2.75639	3.6594
30	0.255605	0.682756	1.310415	1.697261	2.04227	2.45726	2.75000	3.6460
inf	0.253347	0.674490	1.281552	1.644854	1.95996	2.32635	2.57583	3.2905



F Table for alpha=0.05



d1/d2	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	INF
1	161.4476	199.5	215.7073	224.5832	230.1619	233.986	236.7684	238.8827	240.5433	241.8817	243.506	245.4599	248.0131	249.0518	250.0951	251.1432	252.1957	253.2529	254.3144
2	18.5128	19	19.1643	19.2468	19.2864	19.3295	19.3532	19.3781	19.3946	19.3989	19.4225	19.4291	19.4458	19.4541	19.4624	19.4707	19.4791	19.4874	19.4957
3	10.128	9.5521	9.2766	9.1172	9.0135	8.9406	8.8867	8.8452	8.8123	8.7855	8.7446	8.7029	8.6602	8.6385	8.6166	8.5948	8.572	8.5494	8.5264
4	7.7086	6.9443	6.5914	6.3882	6.2561	6.1631	6.0942	6.041	5.9998	5.9644	5.9117	5.8528	5.8025	5.7744	5.7444	5.712	5.6877	5.6581	5.6281
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725	4.7351	4.6777	4.6188	4.5591	4.5272	4.4957	4.4638	4.4314	4.3985	4.365
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2067	4.1468	4.099	4.06	3.9959	3.9381	3.8742	3.8415	3.8082	3.7743	3.7398	3.7047	3.6699
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.866	3.787	3.7257	3.6767	3.6365	3.5747	3.5107	3.4445	3.4105	3.3758	3.3404	3.3043	3.2674	3.2298
8	5.3177	4.459	4.0662	3.8379	3.6875	3.5806	3.5005	3.4381	3.3891	3.3472	3.2839	3.2184	3.1503	3.1152	3.0794	3.0428	3.0053	2.9669	2.9276
9	5.1174	4.2565	3.8625	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789	3.1373	3.0729	3.0061	2.9365	2.9005	2.8637	2.8259	2.7872	2.7475	2.7067
10	4.9646	4.1028	3.7083	3.478	3.3258	3.2172	3.1355	3.0717	3.0204	2.9782	2.913	2.845	2.774	2.7372	2.6996	2.6609	2.6211	2.5801	2.5379
11	4.8443	3.9823	3.5874	3.3567	3.2039	3.0946	3.0123	2.948	2.8962	2.8536	2.7876	2.7186	2.6464	2.609	2.5705	2.5309	2.4901	2.448	2.4045
12	4.7472	3.8853	3.4903	3.2592	3.1059	2.9961	2.9134	2.8485	2.7964	2.7534	2.6866	2.6169	2.5436	2.5055	2.4653	2.4259	2.3842	2.341	2.2961
13	4.6672	3.8056	3.4105	3.1791	3.0254	2.9153	2.8321	2.7669	2.7144	2.671	2.6037	2.5331	2.4589	2.4202	2.3803	2.3392	2.2966	2.2524	2.2064
14	4.6001	3.7389	3.3439	3.1122	2.9582	2.8477	2.7642	2.6987	2.6458	2.6022	2.5342	2.463	2.3879	2.3482	2.3067	2.2644	2.2219	2.1778	2.1307
15	4.5431	3.6823	3.2874	3.0556	2.9013	2.7905	2.7066	2.6408	2.5876	2.5437	2.4753	2.4034	2.3275	2.2878	2.2458	2.2033	2.1601	2.1141	2.0658
16	4.494	3.6337	3.2389	3.0069	2.8524	2.7413	2.6572	2.5911	2.5377	2.4935	2.4247	2.3522	2.2756	2.2354	2.1938	2.1507	2.1058	2.0589	2.0096
17	4.4513	3.5915	3.1968	2.9647	2.8101	2.6987	2.6143	2.548	2.4943	2.4499	2.3807	2.3077	2.2304	2.1898	2.1477	2.104	2.0584	2.0107	1.9604
18	4.4139	3.5546	3.1599	2.9277	2.7729	2.6613	2.5767	2.5102	2.4563	2.4117	2.3421	2.2686	2.1906	2.1497	2.1071	2.0629	2.0166	1.9681	1.9168
19	4.3807	3.5219	3.1274	2.8951	2.7401	2.6283	2.5435	2.4768	2.4227	2.3779	2.308	2.2341	2.1555	2.1141	2.0712	2.0264	1.9795	1.9302	1.878
20	4.3512	3.4928	3.0984	2.8661	2.7109	2.599	2.514	2.4471	2.3928	2.3479	2.2776	2.2033	2.1242	2.0825	2.0391	1.9938	1.9464	1.8963	1.8437
21	4.3248	3.4668	3.0725	2.8401	2.6848	2.5727	2.4876	2.4205	2.366	2.321	2.2504	2.1757	2.096	2.054	2.0102	1.9645	1.9155	1.8637	1.811
22	4.3009	3.4434	3.0491	2.8167	2.6613	2.5491	2.4638	2.3965	2.3419	2.2967	2.2258	2.1508	2.0707	2.0283	1.9842	1.938	1.8894	1.838	1.7831
23	4.2793	3.4221	3.0278	2.7953	2.64	2.5277	2.4422	2.3748	2.3201	2.2747	2.2036	2.1282	2.0476	2.005	1.9605	1.9139	1.8648	1.8128	1.757
24	4.2597	3.4028	3.0088	2.7763	2.6207	2.5082	2.4226	2.3551	2.3002	2.2547	2.1834	2.1077	2.0267	1.9838	1.939	1.892	1.8424	1.7896	1.733
25	4.2417	3.3852	2.9912	2.7587	2.603	2.4904	2.4047	2.3371	2.2821	2.2365	2.1649	2.0885	2.0075	1.9643	1.9192	1.8718	1.8217	1.7684	1.711
26	4.2252	3.369	2.9752	2.7426	2.5868	2.4741	2.3883	2.3205	2.2655	2.2197	2.1479	2.0716	1.9908	1.9464	1.901	1.8533	1.8027	1.7488	1.6906
27	4.21	3.3541	2.9604	2.7278	2.5719	2.4591	2.3732	2.3053	2.2501	2.2043	2.1323	2.0558	1.9746	1.9299	1.8842	1.8351	1.7851	1.7306	1.6717
28	4.196	3.3404	2.9467	2.7141	2.5581	2.4453	2.3593	2.2913	2.236	2.19	2.1179	2.0411	1.9596	1.9147	1.8687	1.8203	1.7699	1.7138	1.6541
29	4.183	3.3277	2.934	2.7014	2.5454	2.4324	2.3463	2.2783	2.2229	2.1768	2.1045	2.0275	1.9456	1.9005	1.8543	1.8055	1.7537	1.6991	1.6376
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107	2.1646	2.0921	2.0148	1.9317	1.8864	1.8409	1.7918	1.7396	1.6835	1.6223
40	4.0847	3.2317	2.8387	2.606	2.4495	2.3359	2.249	2.1802	2.124	2.0772	2.0035	1.9255	1.8389	1.7929	1.7444	1.6928	1.6373	1.5766	1.5089
60	4.0012	3.1504	2.7581	2.5252	2.3683	2.2541	2.1655	2.097	2.0401	1.9925	1.9174	1.8354	1.748	1.7001	1.6491	1.5943	1.5349	1.4673	1.3895
120	3.9201	3.0718	2.6802	2.4472	2.2899	2.175	2.0868	2.018	2.0606	1.995	1.9205	1.8375	1.7505	1.7016	1.6484	1.591	1.5319	1.4639	1.385
INF	3.8415	2.9957	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799	1.8307	1.7552	1.6664	1.5705	1.5213	1.4591	1.394	1.318	1.2214	1